Université Libanaise
Faculté d'Information
Br I

الجامعة اللبنانية
كلية الاعلام
الفرع الاول

الامتحانات النهائية للفصل الأول

Final round 2 2018-2019

السنة المنهجية: الاولى	المادة: Statistics and probability
الاختصاص: Data science	المدة:120 د
	الأستاذ: د. مروى الحاج

Exercise 1 (4 points):
The lengths of service of all the executives employed by Standard Chemicals are:

Name	Years
Mr. Snow	20
Mr. Tolson	22
Mr. Kraft	26
Ms. Irwin	24
Mr. John	28

a) How many different samples of 4 are possible?
b) List all possible samples of size 4, and compute the mean number of cases in each sample.
c) Compare the mean of the distribution of sample means to the population mean.

Exercise 2 (4 points):

The rent for a car Audi A8 follows the normal distribution with a mean of $50 per hour and a standard deviation of $30 per hour. We select a sample of 9 cars.
a) What can we say about the shape of the distribution of the sample mean?
b) What is the standard error of the mean in this example?
c) What is the likelihood the sample mean is greater than $60?
d) What is the likelihood the sample mean is between $40 and $60?

Exercise 3 (3 points):

It is reported that 8 percent of products produced by Concord industry are defected. In a sample of 60 products, and by using the Poisson probability distribution find:

a) The mean and standard deviation of the distribution
b) The probability that none of the product is defected?
c) The probability that at least three products are defected?

Exercise 4 (5 points):

The waiting time for customers at Noura Restaurant follows a normal distribution. A sample of 36 observations is selected. The sample mean is 21 minutes and the population standard deviation is 5 minutes. Conduct the following test of hypothesis using the 0.05 significance level.

$$H_0 : \mu \leq 20$$
$$H_1 : \mu > 20$$

a) Can we use *z* as the test statistic? Tell why or why not.
b) Show the decision rule graphically.
c) State your decision regarding the null hypothesis.
d) What is the p-value?

Exercise 5 (4 points):

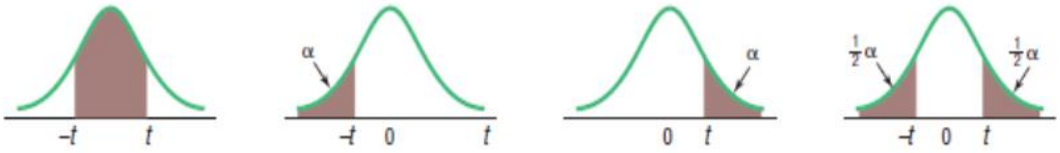
A sample of 65 observations is selected from one population with a population standard
deviation of 0.75. The sample mean is 2.67. A sample of 50 observations is selected from a second population with a population standard deviation of 0.66. The sample mean is 2.59. Conduct the following test of hypothesis using the .08 significance level.

$$H_0: \mu_1 \leq \mu_2$$
$$H_1: \mu_1 > \mu_2$$

a) Is this a one-tailed or a two-tailed test?
b) State the decision rule.
c) Compute the value of the test statistic.
d) What is your decision regarding H_0?

Good luck

B.2 Student's *t* Distribution

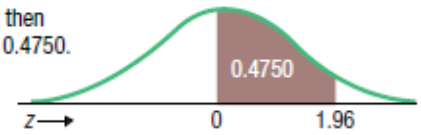


	Confidence Intervals, *c*					
	80%	90%	95%	98%	99%	99.9%
	Level of Significance for One-Tailed Test, α					
df	0.10	0.05	0.025	0.01	0.005	0.0005
	Level of Significance for Two-Tailed Test, α					
	0.20	0.10	0.05	0.02	0.01	0.001
1	3.078	6.314	12.706	31.821	63.657	636.619
2	1.886	2.920	4.303	6.965	9.925	31.599
3	1.638	2.353	3.182	4.541	5.841	12.924
4	1.533	2.132	2.776	3.747	4.604	8.610
5	1.476	2.015	2.571	3.365	4.032	6.869
6	1.440	1.943	2.447	3.143	3.707	5.959
7	1.415	1.895	2.365	2.998	3.499	5.408
8	1.397	1.860	2.306	2.896	3.355	5.041
9	1.383	1.833	2.262	2.821	3.250	4.781
10	1.372	1.812	2.228	2.764	3.169	4.587
11	1.363	1.796	2.201	2.718	3.106	4.437
12	1.356	1.782	2.179	2.681	3.055	4.318
13	1.350	1.771	2.160	2.650	3.012	4.221
14	1.345	1.761	2.145	2.624	2.977	4.140
15	1.341	1.753	2.131	2.602	2.947	4.073
16	1.337	1.746	2.120	2.583	2.921	4.015
17	1.333	1.740	2.110	2.567	2.898	3.965
18	1.330	1.734	2.101	2.552	2.878	3.922
19	1.328	1.729	2.093	2.539	2.861	3.883
20	1.325	1.725	2.086	2.528	2.845	3.850
21	1.323	1.721	2.080	2.518	2.831	3.819
22	1.321	1.717	2.074	2.508	2.819	3.792
23	1.319	1.714	2.069	2.500	2.807	3.768
24	1.318	1.711	2.064	2.492	2.797	3.745
25	1.316	1.708	2.060	2.485	2.787	3.725
26	1.315	1.706	2.056	2.479	2.779	3.707
27	1.314	1.703	2.052	2.473	2.771	3.690
28	1.313	1.701	2.048	2.467	2.763	3.674
29	1.311	1.699	2.045	2.462	2.756	3.659
30	1.310	1.697	2.042	2.457	2.750	3.646
31	1.309	1.696	2.040	2.453	2.744	3.633
32	1.309	1.694	2.037	2.449	2.738	3.622
33	1.308	1.692	2.035	2.445	2.733	3.611
34	1.307	1.691	2.032	2.441	2.728	3.601
35	1.306	1.690	2.030	2.438	2.724	3.591

	Confidence Intervals, *c*					
	80%	90%	95%	98%	99%	99.9%
	Level of Significance for One-Tailed Test, α					
df	0.10	0.05	0.025	0.01	0.005	0.0005
	Level of Significance for Two-Tailed Test, α					
	0.20	0.10	0.05	0.02	0.01	0.001
36	1.306	1.688	2.028	2.434	2.719	3.582
37	1.305	1.687	2.026	2.431	2.715	3.574
38	1.304	1.686	2.024	2.429	2.712	3.566
39	1.304	1.685	2.023	2.426	2.708	3.558
40	1.303	1.684	2.021	2.423	2.704	3.551
41	1.303	1.683	2.020	2.421	2.701	3.544
42	1.302	1.682	2.018	2.418	2.698	3.538
43	1.302	1.681	2.017	2.416	2.695	3.532
44	1.301	1.680	2.015	2.414	2.692	3.526
45	1.301	1.679	2.014	2.412	2.690	3.520
46	1.300	1.679	2.013	2.410	2.687	3.515
47	1.300	1.678	2.012	2.408	2.685	3.510
48	1.299	1.677	2.011	2.407	2.682	3.505
49	1.299	1.677	2.010	2.405	2.680	3.500
50	1.299	1.676	2.009	2.403	2.678	3.496
51	1.298	1.675	2.008	2.402	2.676	3.492
52	1.298	1.675	2.007	2.400	2.674	3.488
53	1.298	1.674	2.006	2.399	2.672	3.484
54	1.297	1.674	2.005	2.397	2.670	3.480
55	1.297	1.673	2.004	2.396	2.668	3.476
56	1.297	1.673	2.003	2.395	2.667	3.473
57	1.297	1.672	2.002	2.394	2.665	3.470
58	1.296	1.672	2.002	2.392	2.663	3.466
59	1.296	1.671	2.001	2.391	2.662	3.463
60	1.296	1.671	2.000	2.390	2.660	3.460
61	1.296	1.670	2.000	2.389	2.659	3.457
62	1.295	1.670	1.999	2.388	2.657	3.454
63	1.295	1.669	1.998	2.387	2.656	3.452
64	1.295	1.669	1.998	2.386	2.655	3.449
65	1.295	1.669	1.997	2.385	2.654	3.447
66	1.295	1.668	1.997	2.384	2.652	3.444
67	1.294	1.668	1.996	2.383	2.651	3.442
68	1.294	1.668	1.995	2.382	2.650	3.439
69	1.294	1.667	1.995	2.382	2.649	3.437
70	1.294	1.667	1.994	2.381	2.648	3.435

B.1 Areas under the Normal Curve

Example:
If $z = 1.96$, then
$P(0 \text{ to } z) = 0.4750$.



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990

$P = F(-t)$	0,000	0,001	0,002	0,003	0,004	0,005	0,006	0,007	0,008	0,009	0,010	
0,00		3,0902	2,8782	2,7478	2,6521	2,5758	2,5121	2,4573	2,4089	2,3656	2,3263	0,99
0,01	2,3263	2,2904	2,2571	2,2262	2,1973	2,1701	2,1444	2,1201	2,0969	2,0749	2,0537	0,98
0,02	2,0537	2,0335	2,0141	1,9954	1,9774	1,9600	1,9431	1,9268	1,9110	1,8957	1,8808	0,97
0,03	1,8808	1,8663	1,8522	1,8384	1,8250	1,8119	1,7991	1,7866	1,7744	1,7624	1,7507	0,96
0,04	1,7507	1,7392	1,7279	1,7169	1,7060	1,6954	1,6849	1,6747	1,6646	1,6546	1,6449	0,95
0,05	1,6449	1,6352	1,6258	1,6164	1,6072	1,5982	1,5893	1,5805	1,5718	1,5632	1,5548	0,94
0,06	1,5548	1,5464	1,5382	1,5301	1,5220	1,5141	1,5063	1,4985	1,4909	1,4833	1,4758	0,93
0,07	1,4758	1,4684	1,4611	1,4538	1,4466	1,4395	1,4325	1,4255	1,4187	1,4118	1,4051	0,92
0,08	1,4051	1,3984	1,3917	1,3852	1,3787	1,3722	1,3658	1,3595	1,3532	1,3469	1,3408	0,91
0,09	1,3408	1,3346	1,3285	1,3225	1,3165	1,3106	1,3047	1,2988	1,2930	1,2873	1,2816	0,90
0,10	1,2816	1,2759	1,2702	1,2646	1,2591	1,2536	1,2481	1,2426	1,2372	1,2319	1,2265	0,89
0,11	1,2265	1,2212	1,2160	1,2107	1,2055	1,2004	1,1952	1,1901	1,1850	1,1800	1,1750	0,88
0,12	1,1750	1,1700	1,1650	1,1601	1,1552	1,1503	1,1455	1,1407	1,1359	1,1311	1,1264	0,87
0,13	1,1264	1,1217	1,1170	1,1123	1,1077	1,1031	1,0985	1,0939	1,0893	1,0848	1,0803	0,86
0,14	1,0803	1,0758	1,0714	1,0669	1,0625	1,0581	1,0537	1,0494	1,0450	1,0407	1,0364	0,85
0,15	1,0364	1,0322	1,0279	1,0237	1,0194	1,0152	1,0110	1,0069	1,0027	0,9986	0,9945	0,84
0,16	0,9945	0,9904	0,9863	0,9822	0,9782	0,9741	0,9701	0,9661	0,9621	0,9581	0,9542	0,83
0,17	0,9542	0,9502	0,9463	0,9424	0,9385	0,9346	0,9307	0,9269	0,9230	0,9192	0,9154	0,82
0,18	0,9154	0,9116	0,9078	0,9040	0,9002	0,8965	0,8927	0,8890	0,8853	0,8816	0,8779	0,81
0,19	0,8779	0,8742	0,8705	0,8669	0,8633	0,8596	0,8560	0,8524	0,8488	0,8452	0,8416	0,80
0,20	0,8416	0,8381	0,8345	0,8310	0,8274	0,8239	0,8204	0,8169	0,8134	0,8099	0,8064	0,79
0,21	0,8064	0,8030	0,7995	0,7961	0,7926	0,7892	0,7858	0,7824	0,7790	0,7756	0,7722	0,78
0,22	0,7722	0,7688	0,7655	0,7621	0,7588	0,7554	0,7521	0,7488	0,7454	0,7421	0,7388	0,77
0,23	0,7388	0,7356	0,7323	0,7290	0,7257	0,7225	0,7192	0,7160	0,7128	0,7095	0,7063	0,76
0,24	0,7063	0,7031	0,6999	0,6967	0,6935	0,6903	0,6871	0,6840	0,6808	0,6776	0,6745	0,75
0,25	0,6745	0,6713	0,6682	0,6651	0,6620	0,6588	0,6557	0,6526	0,6495	0,6464	0,6433	0,74
0,26	0,6433	0,6403	0,6372	0,6341	0,6311	0,6280	0,6250	0,6219	0,6189	0,6158	0,6128	0,73
0,27	0,6128	0,6098	0,6063	0,6038	0,6008	0,5978	0,5948	0,5918	0,5888	0,5858	0,5828	0,72
0,28	0,5828	0,5799	0,5769	0,5740	0,5710	0,5681	0,5651	0,5622	0,5592	0,5563	0,5534	0,71
0,29	0,5534	0,5505	0,5476	0,5446	0,5417	0,5388	0,5359	0,5330	0,5302	0,5273	0,5244	0,70
0,30	0,5244	0,5215	0,5187	0,5158	0,5129	0,5101	0,5072	0,5044	0,5015	0,4987	0,4959	0,69
0,31	0,4959	0,4930	0,4902	0,4874	0,4845	0,4817	0,4789	0,4761	0,4733	0,4705	0,4677	0,68
0,32	0,4677	0,4649	0,4621	0,4593	0,4565	0,4538	0,4510	0,4482	0,4454	0,4427	0,4399	0,67
0,33	0,4399	0,4372	0,4344	0,4316	0,4289	0,4261	0,4234	0,4207	0,4179	0,4152	0,4125	0,66
0,34	0,4125	0,4097	0,4070	0,4043	0,4016	0,3989	0,3961	0,3934	0,3907	0,3880	0,3853	0,65
0,35	0,3853	0,3826	0,3799	0,3772	0,3745	0,3719	0,3692	0,3665	0,3638	0,3611	0,3585	0,64
0,36	0,3585	0,3558	0,3531	0,3505	0,3478	0,3451	0,3425	0,3398	0,3372	0,3345	0,3319	0,63
0,37	0,3319	0,3292	0,3266	0,3239	0,3213	0,3186	0,3160	0,3134	0,3107	0,3081	0,3055	0,62
0,38	0,3055	0,3029	0,3002	0,2976	0,2950	0,2924	0,2898	0,2871	0,2845	0,2819	0,2793	0,61
0,39	0,2793	0,2767	0,2741	0,2715	0,2689	0,2663	0,2637	0,2611	0,2585	0,2559	0,2533	0,60
0,40	0,2533	0,2506	0,2482	0,2456	0,2430	0,2404	0,2378	0,2353	0,2327	0,2301	0,2275	0,59
0,41	0,2275	0,2250	0,2224	0,2198	0,2173	0,2147	0,2121	0,2096	0,2070	0,2045	0,2019	0,58
0,42	0,2019	0,1993	0,1968	0,1942	0,1917	0,1891	0,1860	0,1840	0,1815	0,1789	0,1764	0,57
0,43	0,1764	0,1738	0,1713	0,1687	0,1662	0,1637	0,1611	0,1586	0,1560	0,1535	0,1510	0,56
0,44	0,1510	0,1484	0,1459	0,1434	0,1408	0,1383	0,1358	0,1332	0,1307	0,1282	0,1257	0,55
0,45	0,1257	0,1231	0,1206	0,1181	0,1156	0,1130	0,1105	0,1080	0,1055	0,1030	0,1004	0,54
0,46	0,1004	0,0979	0,0954	0,0929	0,0904	0,0878	0,0853	0,0828	0,0803	0,0778	0,0753	0,53
0,47	0,0753	0,0728	0,0702	0,0677	0,0652	0,0627	0,0602	0,0557	0,0552	0,0527	0,0502	0,52
0,48	0,0502	0,0476	0,0451	0,0426	0,0401	0,0376	0,0351	0,0326	0,0301	0,0276	0,0251	0,51
0,49	0,0251	0,0226	0,0201	0,0175	0,0150	0,0125	0,0100	0,0075	0,0050	0,0025	0,0000	0,50
	0,010	0,009	0,008	0,007	0,006	0,005	0,004	0,003	0,002	0,001	0,000	$P = F(t)$